

Two-scale scalar mesons in nuclei

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Abstract

We generalize the linear σ model in order to develop a chiral-invariant model of nuclear structure. The model is *natural*, and contains not only the usual σ meson which is the chiral partner of the pion but also a new chiral-singlet that is responsible for the medium-range nucleon-nucleon attraction. This approach provides significant advantages in terms of its description of nuclear matter and finite nuclei in comparison with conventional models based on the linear σ model.

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Phenomenological relativistic field theories can provide a satisfactory description of the properties of nuclear matter and finite nuclei [1,2]. The fundamental importance of chiral symmetry means that it must be incorporated into models of this kind. As a result, there is a long history of attempts to generalize the linear σ model ($L\sigma M$) to build nuclear models with chiral symmetry. However, it is well known that the $L\sigma M$, supplemented by a repulsive force associated with ω -exchange, leads to bifurcations in the equation of state (EOS) [3,4] and that the model usually gives a very large incompressibility, K , and, hence, a very stiff EOS. The bifurcation problem may be settled (1) by introducing a σ - ω coupling in the mean-field approximation (MFA) [4] and (2) in the one-loop approximation due to a modified effective potential [5].

It is, however, difficult to build relativistic mean field phenomenology with manifest chiral symmetry based upon the conventional $L\sigma M$, which contains a scalar meson (namely the σ meson) playing a dual role as the chiral partner of the pion *and* the mediator of the medium-range nucleon-nucleon (NN) attraction [6]. Chiral perturbation theory actually forbids the identification of this NN attraction with the exchange of the σ . In the $L\sigma M$, two critical constraints are imposed: one is the “Mexican hat” potential, which gives a very strong nonlinearity of the scalar field, and the other is the equality between the scalar and pion couplings to the nucleon. The latter eventually requires a large value ($\geq 600\text{MeV}$) of the σ mass and leads to unrealistic, oscillating nuclear charge densities, level ordering and shell closures [6]. Furthermore, as is well known, the predictions of the $L\sigma M$ generally involve cancellations among several graphs. One example is the πN scattering amplitude where the σ exchange combining with the Born term satisfies the soft pion results, whose magnitude is too small.

An alternative is to adopt a nonlinear realization of chiral symmetry. To avoid the unnatural cancellations of the $L\sigma M$, the σ field is eliminated by imposing the constraint that the fields lie on the chiral circle, $\sigma^2 + \vec{\pi}^2 = f_\pi^2$ (with f_π the pion decay constant), in the nonlinear model (NLM). This is all fine for chiral symmetry. However, at mean-field level, it is somewhat frustrating for nuclear physics because it is not easy to introduce a scalar-isoscalar channel which is responsible for the mid-range NN attraction. When studying only elementary processes, the cancellations are just a matter of taking care but when studying the nuclear many-body problem in MFA, it is certainly much simpler to introduce a scalar-isoscalar meson explicitly.

In the usual NLM, the chiral radius is fixed to f_π by mere convenience. However, nothing prevents us from keeping the fluctuation of the chiral circle as a degree of freedom, and identifying it with the meson which yields the mid-range attraction. Chanfray et al. [7] have proposed a chiral nuclear model in which the $L\sigma M$ is reformulated in the standard nonlinear form as far as the pion field is concerned but where the scalar degree of freedom (called θ), corresponding to fluctuations along the chiral radius, is maintained. Thus, the model explicitly involves the scalar meson for the NN attraction but does not have the unnatural cancellations. However, in their calculation the mass of the θ meson was predicted to be in the range $0.8 - 1.0$ GeV, which may again be too large to obtain good fits to the properties of finite nuclei.

Combining nonlinear chiral symmetry with the broken scale invariance of QCD is another approach to construct a nuclear model [8]. In such a model, the low-energy theorems involving the QCD trace anomaly of the energy-momentum tensor are *assumed* to be saturated by

a scalar glueball (gluonium) field with a large (above 1 GeV) mass *and* a light scalar field. Thus, two different scales are required in the scalar channel. After integrating out the heavy gluonium field, one can construct an effective model which contains the chiral-singlet scalar field with a mass of about 400-500 MeV. Since the light scalar meson can be responsible for the mid-range NN attraction, the model provides good fits to the bulk properties of finite nuclei and single-particle spectra. However, this does not involve the scalar field which corresponds to the fluctuation of the chiral radius.

Even in the $L\sigma M$, if a new, light scalar field which phenomenologically simulates the mid-range attractive NN force is introduced not as the chiral partner of the pion but as a chiral singlet, one may be able to construct a new chiral-invariant model. Here we construct such a model and study the role of scalar mesons in symmetric nuclear matter as well as finite nuclei. As discussed above, it may be necessary to include at least two kinds of scalar mesons: one the usual σ meson with a relatively large mass and the other a new, chiral-singlet scalar meson with a light mass. The σ meson is the chiral partner of the pion and they form an isoscalar-isovector scalar quartet, $(\sigma, \vec{\pi})$. The fluctuations around the stable point on the chiral circle are described by them. When the σ mass is large, the σ field itself is relatively reduced in matter and it is hence expected that the “Mexican hat” potential producing the undesirable, strong nonlinearity of the σ field would also be suppressed. In contrast, because of its small mass, the new scalar field is enhanced and it may provide the main part of the NN attraction. Our underlying philosophy is that the NN attraction in matter is simply dominated by scalar-isoscalar, correlated two-pion exchange and that it is this that is being simulated by the light scalar meson in MFA.

Let us first start from the Lagrangian density of the $L\sigma M$ with an explicit symmetry breaking term

$$\mathcal{L} = \mathcal{L}_0 + \mathcal{L}_{SB}, \quad (1)$$

where

$$\mathcal{L}_0 = \bar{\psi}[i\gamma^\mu\partial_\mu - g_0(\sigma + i\vec{\tau} \cdot \vec{\pi}\gamma_5)]\psi + \frac{1}{2}(\partial_\mu\sigma\partial^\mu\sigma + \partial_\mu\vec{\pi} \cdot \partial^\mu\vec{\pi}) - \frac{\lambda}{4}(\sigma^2 + \vec{\pi}^2 - v^2)^2, \quad (2)$$

and $\mathcal{L}_{SB} = c\sigma$ with σ and $\vec{\pi}$ the σ and π fields, respectively. Next we introduce a chiral-invariant Lagrangian density for the chiral-singlet scalar meson s :

$$\mathcal{L}_s = \frac{g_s}{f_\pi}\bar{\psi}(\sigma + i\vec{\tau} \cdot \vec{\pi}\gamma_5)F(s)\psi + \frac{1}{2}(\partial_\mu s\partial^\mu s - m_s^2 s^2), \quad (3)$$

with g_s the strength of the s -N coupling and m_s the s -meson mass. The first term describes the interaction between the s meson and nucleon, which is similar to that adopted in Eq.(20) of Ref. [9]. In general, $F(s)$ is allowed to be an arbitrary function of the scalar field. However, in the present model we choose the simplest one, namely, $F(s) = s$. Note that, as demonstrated in the QMC model [10,11], this complexity is associated with the fact that the nucleon has the internal structure which responds to the mean scalar fields. In principle one could also multiply this interaction by an arbitrary function of $\sigma^2 + \vec{\pi}^2$. However, since the σ field is relatively suppressed because of its large mass, we ignore such possibilities in this initial investigation. We simply add this Lagrangian density with $F(s) = s$ to the $L\sigma M$.

It is also vital to add the repulsive NN interaction due to the ω -meson exchange. It can be introduced as a gauge-like boson [4], that is, we add the kinetic energy term for the ω meson and replace the derivative by a covariant form: $\partial_\mu \rightarrow D_\mu = \partial_\mu + ig_v \omega_\mu$, with g_v the ω -N coupling constant.

As usual, we shift the σ field ($\sigma \rightarrow f_\pi - \sigma$) and eliminate λ , v and c in favor of the free masses of the nucleon, σ and π mesons (M , m_σ and m_π , respectively). (Notice that hereafter σ denotes the shifted, positive mean value.) The free masses are generated by spontaneous symmetry breaking. Taking MFA, the total Lagrangian density then reads

$$\begin{aligned} \mathcal{L} = & \bar{\psi}[i\gamma^\mu \partial_\mu - M^*(\sigma, s) - g_v \gamma_0 \omega]\psi + \frac{1}{2}(\partial_\mu \sigma \partial^\mu \sigma + \partial_\mu s \partial^\mu s) - \frac{1}{2}(m_\sigma^2 \sigma^2 + m_s^2 s^2) \\ & - \frac{1}{2}\partial_\mu \omega \partial^\mu \omega + \frac{1}{2}m_\omega^{*2}(\sigma, s)\omega^2 - V(\sigma), \end{aligned} \quad (4)$$

where the pion field vanishes, because the nuclear ground state has good parity. The time component of the ω field is simply denoted by ω and the ‘‘Mexican hat’’ potential, V , is

$$V(\sigma) = \frac{1-R}{8} \left(\frac{m_\sigma}{f_\pi} \right)^2 \sigma^3 (\sigma - 4f_\pi), \quad (5)$$

with $R = (m_\pi/m_\sigma)^2$ and $m_\pi (= 138 \text{ MeV})$ the pion mass. In the chiral limit, R becomes 0.

The effective nucleon and ω meson masses are respectively given by

$$M^*(\sigma, s) = (M - g_s s) \left(1 - \frac{\sigma}{f_\pi} \right) = M - g_0 \sigma - g_s s + \frac{1}{M}(g_0 \sigma)(g_s s), \quad (6)$$

$$m_\omega^{*2}(\sigma, s) = m_\omega^2 \left[\left(1 - \frac{\sigma}{f_\pi} \right)^2 + \left(\frac{s}{f_\pi} \right)^2 \right]. \quad (7)$$

Here the free masses and the pion decay constant in vacuum are taken to be $M = 939 \text{ MeV}$, $m_\omega = 783 \text{ MeV}$ and $f_\pi = 93 \text{ MeV}$. Because the pion decay constant is fixed, the coupling constants g_0 and g_v are automatically determined through the relations $M = f_\pi g_0$ and $m_\omega = g_v f_\pi$.

This gives the total energy per nucleon (for symmetric nuclear matter) at baryon density ρ_B :

$$\frac{E}{A} = \frac{4}{(2\pi)^3 \rho_B} \int d\vec{k} \sqrt{M^{*2} + \vec{k}^2} + \frac{1}{2\rho_B}(m_\sigma^2 \sigma^2 + m_s^2 s^2) + \frac{g_v^2 \rho_B}{2m_\omega^{*2}} + \frac{V(\sigma)}{\rho_B}. \quad (8)$$

There are three parameters to be determined: the scalar meson masses, m_σ and m_s , and the coupling constant g_s . First, let us try to fix m_σ to be a relatively large mass around 1 GeV. The remaining parameters, m_s and g_s , are then chosen so as to produce the saturation property of symmetric nuclear matter: $E/A - M = -15.7 \text{ MeV}$ at $\rho_0 = 0.17 \text{ fm}^{-3}$ (ρ_0 the normal nuclear matter density).

This Lagrangian, however, produces a very small incompressibility, around 100 MeV. As seen in Eq.(7), the coupling of the σ meson to the ω reduces the ω mass in matter, while the light scalar meson enhances it. Since the ω mass is eventually not reduced much at large ρ_B , the repulsive force is insufficient and the model cannot produce the correct incompressibility

($K = 210 \pm 30$ MeV). If the effective ω mass is reduced significantly, the EOS becomes stiff [12]. To cure this defect, let us add a (chiral-invariant) term

$$\mathcal{L}_{new} = -\frac{\zeta}{2f_\pi} g_v^2 \omega^2 s^3, \quad (9)$$

to the Lagrangian density. This term changes the effective ω meson mass as

$$m_\omega^{*2} = m_\omega^2 \left[\left(1 - \frac{\sigma}{f_\pi}\right)^2 + \left(1 - \zeta \frac{s}{f_\pi}\right) \left(\frac{s}{f_\pi}\right)^2 \right]. \quad (10)$$

The new parameter ζ can control m_ω^* around ρ_0 and provide a more realistic incompressibility. Eq.(10) also implies that, as in the nucleon, the ω meson has internal structure which depends on the scalar fields [11].

Now we are in a position to show our results for nuclear matter. Varying the σ meson mass, we determine the three parameters, m_s , g_s and ζ , so as to reproduce the saturation condition and the correct K . In Table I, we show the nuclear matter properties at ρ_0 . We also present the scalar and vector mean fields as functions of nuclear matter density in Fig.1. In our calculation, the σ mass varies around 1 GeV. As discussed above, the mass of the light scalar meson should be about 400 – 500 MeV to get good fits to properties of finite nuclei. From the table, in the case of $m_\sigma = 1.0 - 1.05$ GeV, the s meson mass is in the desired range. This is not a trivial fact. In contrast, in the case where $m_\sigma \geq 1.1$ GeV ($m_\sigma \leq 0.95$ GeV), m_s seems too large (small). Furthermore, as expected, with increasing σ mass, the contribution of the σ field to the total energy is suppressed (see the table and figure) and the “Mexican hat” potential is correspondingly much reduced. Note that, in the chiral model of Boguta [4], we find $g_0\sigma \simeq 200$ MeV and $V/\rho_B \simeq -21$ MeV at ρ_0 .

The nucleon mass is reduced by about 25% at ρ_0 . In Eq.(6), the linear terms of the scalar fields reduce the mass while the quadratic term increases it. It should be emphasized here that the reduction of the nucleon mass depends on the s field as well as the σ , where the σ may be directly related to the change of quark condensate in matter (see discussions below), while the s -meson contribution is related to the mid-range NN attractive force. In this model, the two different origins of the mass reduction are simultaneously present.

The contribution of the quadratic term in M^* has already been studied in detail in the QMC model from the point of view of the quark substructure of the nucleon [10,11]. In the QMC model, the effective nucleon mass is approximated as $M^* \approx M - g_s s + \frac{a}{2}(g_s s)^2$, where the coefficient of the quadratic term, $a/2$, is known as the scalar polarizability [10,13] (a is estimated to be 10^{-3} MeV $^{-1}$ [11]). In the present case, since numerically $g_0\sigma \simeq 0.5 \times g_s s$ for the proper σ mass (see the table I), the scalar polarizability is of order $1/2M \simeq 0.5 \times 10^{-3}$ MeV $^{-1}$, which is just the same as that in the QMC model.

We now wish to relate the change of the nucleon mass to the evolution of the quark condensate $\langle \bar{q}q(\rho_B) \rangle$ in matter. The quark condensate and its evolution at finite density can be obtained by identifying the symmetry breaking pieces of QCD with that of our Lagrangian: $-2m_q \bar{q}q = c\sigma = f_\pi m_\pi^2 \sigma$. This shows that the condensate evolution is driven by the mean value of σ , the chiral partner of the pion. From this relation and the Gell-Mann-Oakes-Renner relation, we get the relative modification of the condensate (to the vacuum value) at finite density

$$\frac{\langle \bar{q}q(\rho_B) \rangle}{\langle \bar{q}q(0) \rangle} = 1 - \frac{\sigma}{f_\pi}. \quad (11)$$

Since both the σ and s fields at low density are exclusively governed by the scalar density of the nucleon field $\langle \bar{\psi}\psi \rangle$

$$\sigma \simeq \frac{g_0}{m_\sigma^2} \langle \bar{\psi}\psi \rangle \quad \text{and} \quad s \simeq \frac{g_s}{m_s^2} \langle \bar{\psi}\psi \rangle, \quad (12)$$

the s field at low density can be related to the σ field

$$s \simeq \left(\frac{g_s}{g_0} \right) \left(\frac{m_\sigma}{m_s} \right)^2 \sigma. \quad (13)$$

Using Eqs.(6), (11) and (13), we can *numerically* relate the nucleon mass at low density to the condensate evolution

$$\frac{M^*}{M} \simeq \frac{\langle \bar{q}q(\rho_B) \rangle}{\langle \bar{q}q(0) \rangle} \left[1 - \left(\frac{g_s m_\sigma}{g_0 m_s} \right)^2 \left(1 - \frac{\langle \bar{q}q(\rho_B) \rangle}{\langle \bar{q}q(0) \rangle} \right) \right]. \quad (14)$$

This rather complicated structure comes from the fact that the mass reduction depends two different sources, both the quark condensate and the NN attractive force.

Next let us show some properties of finite nuclei. As an illustrative example we consider the case of ^{40}Ca . Firstly, instead of $\rho_0 = 0.17 \text{ fm}^{-3}$, we adopt the value of $\rho_0 = 0.155 \text{ fm}^{-3}$, which is closer to the interior density of ^{208}Pb , and again search the parameter set for nuclear matter. We then find: $m_\sigma = 0.92 \text{ GeV}$, $m_s = 404.0 \text{ MeV}$, $g_s^2 = 18.07$ and $\zeta = 0.7$, which reproduces the saturation condition with $K = 218 \text{ MeV}$. We next solve a set of coupled nonlinear differential equations for a finite nucleus, that is derived from the total Lagrangian density (see Eqs.(4) and (9)). It may be solved by a standard iteration procedure [10,11]. This leads to a value for the binding energy per nucleon of $E_B/A = -8.28 \text{ MeV}$ (the observed value is -8.45 MeV).

In Table II, the calculated spectra are summarized. Because of the relatively smaller scalar and vector fields in the present model than in Quantum Hadrodynamics (QHD) [1], the spin-orbit splittings are smaller. The good agreement in the binding energy per nucleon comes at the expense of a reduction in the spin-orbit force. Note that there is a strong correlation between the effective nucleon mass and the spin-orbit force. It is expected that the inclusion of the exchange contributions (Fock terms) will increase the absolute values of the single-particle, scalar and vector potentials [14]. This increase, together with the contribution to the spin-orbit force from the Fock term itself, may be expected to improve the spin-orbit splitting in finite nuclei. We leave this for a future study.

The charge density distribution is illustrated in Fig.2. Having solved the coupled differential equations, we obtain the point-proton and neutron densities in a nucleus. It is then necessary to consider the effect of the nucleon form factor that gives a considerable correction to the density distribution. We calculate the charge density by a convolution of the point-proton and neutron densities with the proton and neutron charge distributions [10,15]. We then obtain the root-mean-square (rms) charge radius ($r_{ch} = 3.44 \text{ fm}$) and the difference between nuclear rms radii for neutrons and protons ($r_n - r_p = -0.157 \text{ fm}$) – the observed values are, respectively, 3.48 fm and $0.05 \pm 0.05 \text{ fm}$.

As seen in the figure, the calculated charge density distribution is close to the experimental area. We note that there are no strong oscillations, even in the charge density of ^{208}Pb . (In conventional nuclear models based on the $L\sigma M$, unrealistic oscillations in the charge density have been reported [6].) In Fig.3, we show the neutron density distribution. Again we find reasonable agreement with the experimental data. The results for the charge and neutron densities in our model are very similar to those of the other chiral models [8].

In general, an effective field theory at low energy contains an infinite number of interaction terms, which incorporate the *compositeness* of hadrons [11]. It is then expected to involve numerous couplings which may be nonrenormalizable. To make sensible calculations, Manohar and Georgi [18] have proposed a systematic way to manage such complicated, effective field theories called “naive dimensional analysis” (NDA). NDA gives rules for assigning a coefficient of the appropriate size to any interaction term in an effective Lagrangian. After extracting the dimensional factors and some appropriate counting factors using NDA, the remaining *dimensionless* coefficients are all assumed to be of order *unity*. This is the so-called *naturalness* assumption. If naturalness is valid, the effective Lagrangian can be truncated at a given order with a reasonable bound on the truncation error for physical observables. Then we can control the effective Lagrangian, at least at the tree level.

Here we use NDA to see whether this model gives natural coefficients. When a generic, interaction Lagrangian density is written as [19]

$$\mathcal{L}_{int.} \sim c_{\ell m n p} \frac{1}{m!n!p!} \left(\frac{\bar{\psi}\Gamma(\tau/2)\psi}{f_\pi^2\Lambda} \right)^\ell \left(\frac{\sigma}{f_\pi} \right)^m \left(\frac{\omega}{f_\pi} \right)^n \left(\frac{s}{f_\pi} \right)^p (f_\pi\Lambda)^2, \quad (15)$$

the overall coupling constant $c_{\ell m n p}$ is dimensionless and of $\mathcal{O}(1)$ if naturalness holds. Here Γ and τ , respectively, stand for a combination of Dirac matrices and isospin operators, and $\Lambda(\sim 1 \text{ GeV})$ is a large mass scale for the strong interaction.

The present model has 10 interaction terms and the result is shown in Table III. Only three coefficients, c_{0023} , c_{0300} and c_{0400} , are close to 3: c_{0023} comes from Eq.(9) while the latter two are for the “Mexican hat” potential. They all are, however, of order unity and almost natural. This model is thus *natural* as an effective field theory for nuclei.

In summary, we have developed a chiral nuclear model which is *natural*, based on the $L\sigma M$. To describe the properties of nuclear matter and finite nuclei at mean-field level, it seems to be necessary to introduce two different scales associated with the scalar mesons: one is the usual σ meson that is the chiral partner of the pion, and the other is a new one that is treated as a chiral-singlet and is responsible for the mid-range NN attraction. The present model has three parameters, which are determined so as to produce the saturation condition at normal nuclear matter density and the proper incompressibility. Then, the model automatically predicts two scalar scales, that is, one concerns the chiral symmetry ($m_\sigma \sim 1 \text{ GeV}$) and the other relates to the NN attraction ($m_s \sim 400 - 500 \text{ MeV}$). Because the σ mass is heavy, the contribution of the σ field to the total energy is relatively suppressed and the “Mexican hat” potential is very much reduced as well. This fact is vital to obtain better fits to the properties of finite nuclei. We have demonstrated the single particle spectra, charge and neutron densities of ^{40}Ca as well as the properties of symmetric nuclear matter. The present approach improves conventional nuclear models based on the $L\sigma M$. As a next step, it would be necessary to extend this approach to include the ρ meson in order to study unstable nuclei and/or dense matter like neutron stars.

It would be of great interest to study, from the point of view of quark substructure of hadrons, the relation between the dependence of hadron masses on the scalar fields in this chiral model and that in the QMC model [10,11]. In particular, if the effective ω mass is sufficiently reduced around normal nuclear matter density, it would be possible to form an ω -nucleus bound state [20] and such exotic states may provide significant information on chiral symmetry restoration (see Eqs.(10) and (11)). Finally, we observe that the σ mass *predicted* in this model is very close to the scalar glueball mass assumed in Ref. [8] (although it was integrated out and does not appear explicitly). Therefore, it would also be very intriguing to study whether there is a deeper connection between the σ and such scalar glueball.

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TABLES

TABLE I. Properties of symmetric nuclear matter at normal nuclear matter density ($\rho_0 = 0.17 \text{ fm}^{-3}$). The σ mass varies in the range of 0.9 and 1.15 GeV. Note that, in the present model, $g_0^2 = 101.9$ and $g_v^2 = 70.89$, which together with the pion decay constant ($f_\pi = 93 \text{ MeV}$) give the free nucleon and ω meson masses. We take $m_\pi = 138 \text{ MeV}$. All masses, energies and incompressibility are quoted in MeV.

m_σ	m_s	g_s^2	ζ	$g_0\sigma$	$g_s s$	$V(\sigma)/\rho_0$	M^*/M	K
900	346.5	12.28	0.7	130	130	-6.69	0.743	214
950	388.0	17.29	0.75	111	143	-4.72	0.747	216
1000	441.7	24.48	0.8	96.4	155	-3.42	0.750	214
1050	510.7	35.00	0.85	84.4	164	-2.55	0.751	214
1100	612.1	53.08	0.85	74.6	172	-1.93	0.752	212
1150	741.9	81.35	0.85	66.5	179	-1.50	0.752	218

TABLE II. Single particle energies for ^{40}Ca . All energies are quoted in MeV.

	$1s_{1/2}$	$1p_{3/2}$	$1p_{1/2}$	$1d_{5/2}$	$1d_{3/2}$	$2s_{1/2}$
proton	-35.8	-24.8	-23.2	-12.7	-10.0	-7.7
neutron	-44.8	-33.2	-31.7	-20.5	-17.9	-15.8

TABLE III. Interaction terms and corresponding (dimensionless) coupling constants for $m_\sigma = 1050 \text{ MeV}$ (see Table I).

term	c_{lmnp}	value
$\bar{\psi}\sigma\psi$	c_{1100}	0.94
$\bar{\psi}s\psi$	c_{1001}	0.55
$\bar{\psi}\sigma s\psi$	c_{1101}	0.55
$\bar{\psi}\gamma_0\omega\psi$	c_{1010}	0.78
$\sigma\omega^2$	c_{0120}	1.2
$\sigma^2\omega^2$	c_{0220}	1.2
$s^2\omega^2$	c_{0022}	1.2
$s^3\omega^2$	c_{0023}	3.1
σ^3	c_{0300}	3.3
σ^4	c_{0400}	3.3

FIGURES

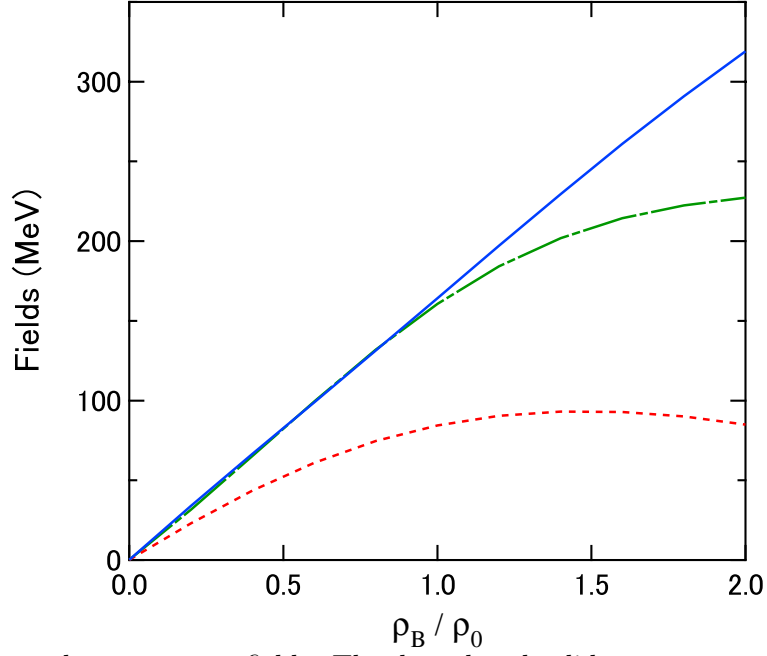


FIG. 1. Scalar and vector mean fields. The dotted and solid curves are, respectively, for the σ ($g_0\sigma$) and s (g_ss) fields, while the dot-dashed one is for the ω ($g_\omega\omega$) field. The σ mass is taken to be 1050 MeV (see Table I).

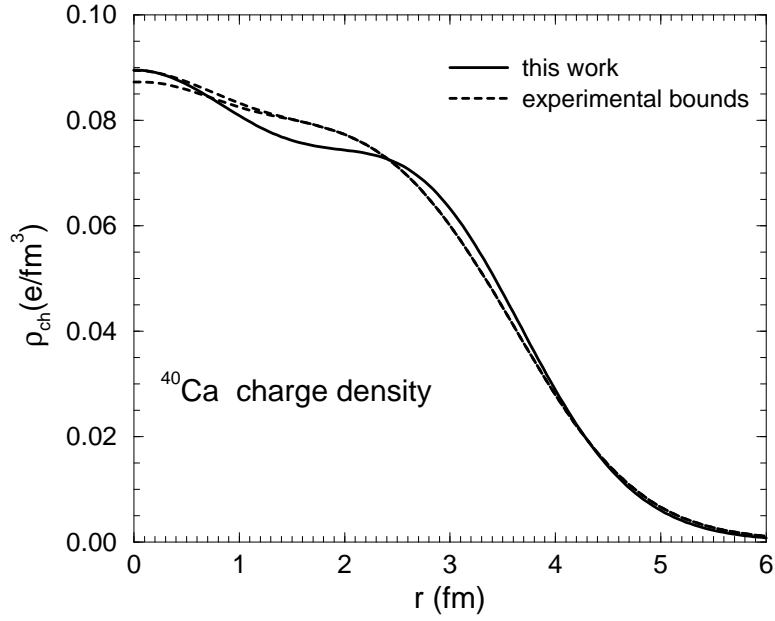


FIG. 2. Charge density distribution for ^{40}Ca . The experimental data are denoted by the dashed area [16].

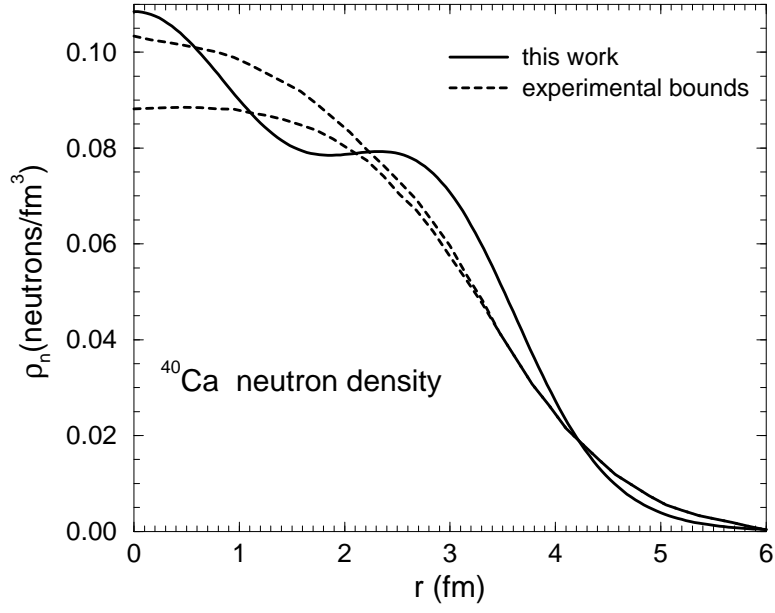


FIG. 3. Point-neutron density distribution in ^{40}Ca . The dashed area represents the empirical fit to proton scattering data performed in Ref. [17].